

Section 4.9 Practice Problems: Antiderivatives

1. Find the antiderivative of the following functions

(a) $f'(x) = \frac{3}{8}x^{1/3} + \frac{7}{11}x^{-1/7}$

(b) $f'(x) = \frac{1}{\sqrt{x}} + \sqrt{x} + \frac{1}{2\sqrt{x}} + \frac{1}{2}\sqrt{x}$

(c) $f'(x) = 6 \cos x - 3 \sin x$

(d) $f'(x) = 5 \sec^2 x + 2 \sec x \tan x$

(e) $f'(x) = 3 \csc^2 x + 4 \csc x \cot x$

(f) $f'(x) = 2 \sinh x + 7 \cosh x$

(g) $f'(x) = \frac{1}{x} + \frac{1}{x^2} + e^x + \frac{1}{3x} - 2e^x$

(h) $f'(x) = \frac{6}{1+x^2} + \frac{2}{\sqrt{1-x^2}} + \frac{1}{\sqrt{4-4x^2}}$

2. Use the indicated initial condition to find the value of c

(a) $f'(x) = 3x^4 - 2x + e^x, f(0) = 3$

(b) $f'(x) = \cos x + \sin x, f(0) = 8$

(c) $f'(x) = \frac{6}{1+x^2}, f\left(\frac{\pi}{4}\right) = 2$

3. A model rocket is launched from a 5 m platform with an upward initial velocity of 75 m/s. Find the equation of motion of the rocket using $g = 10$.
4. A frustrated student throws her textbook out of her apartment window (which is 50 ft above the ground) with an initial downward velocity of 10 ft/s. How long does it take for the textbook to hit the ground? This one is harder; start by finding the equation of motion for $s(t)$. The book hits the ground when $s(t) = 0$, so solve for t .