

$$2. \quad L_4 = \lim_{x \rightarrow 0} \frac{\sqrt{5+x} - \sqrt{5}}{x} \cdot \frac{\sqrt{5+x} + \sqrt{5}}{\sqrt{5+x} + \sqrt{5}} \quad \leftarrow \text{correction}$$

$$= \lim_{x \rightarrow 0} \frac{(\sqrt{5+x})^2 - (\sqrt{5})^2}{x (\sqrt{5+x} + \sqrt{5})}$$

$$= \lim_{x \rightarrow 0} \frac{(5+x) - 5}{x (\sqrt{5+x} + \sqrt{5})}$$

$$= \lim_{x \rightarrow 0} \frac{x}{x (\sqrt{5+x} + \sqrt{5})}$$

$$= \lim_{x \rightarrow 0} \frac{1}{\sqrt{5+x} + \sqrt{5}}$$

$$= \frac{1}{\sqrt{5} + \sqrt{5}} = \frac{1}{2\sqrt{5}}$$