

# **Solidification, Crystal Growth and Casting**

## **Faculty Collaborators**

A. Chait (NASA Glenn Research Center)  
S. H. Davis (Engineering Sciences and Applied Mathematics, Northwestern Univ)  
C. B. Clemons (Theoretical and Applied Mathematics, Univ of Akron)  
D. Golovaty (Theoretical and Applied Mathematics, Univ of Akron)  
S. I. Hariharan (Electrical Eng, Univ of Akron)  
J. Heminger (Theoretical and Applied Mathematics, Univ of Akron)

## **Graduate Students – Masters Theses Directed**

Jeffrey Bonfiglio  
Mikal Gilger  
Teng Li  
Bin Liu  
Pei Qing Luo  
Stephanie Morman  
Lance Nelson  
Jane Zhang

## **Undergraduate Students – Honors Projects Directed**

James DiLellio  
Laurie Humphreys  
Kevin Kupchella  
Brian McDonald  
Jason McHood  
Carl Stitz  
Robert Streharsky  
Gary Traicoff  
Jeffrey Umlauf  
Mira Vukelic

## **Undergraduate Students – Honors Projects In Progress**

Corey Simon

## **Overview of Current Investigations**

Directional solidification techniques are the most widely used methods for preparing high quality single crystals of metallic, electronic, and opto-electronic materials. In order to obtain optimum microstructure and properties in the solidified material, it is important to maintain a uniform distribution of solute/dopants and a flat solidification interface during a growth process. Such ideal conditions are difficult to achieve in practice because of an unavoidable heat exchange between the crucible and the sample. This heat exchange leads to radial temperature gradients and subsequent fluid flow. The results are non-planar solidification fronts and potentially severe axial and radial solute segregation.

Since there is a close relationship between growth conditions and the microstructure and properties of solidified materials, there has been an extensive amount of investigation of

both sharp-interface and phase-field, directional solidification configurations. Exact solutions to these classes of problems are generally restricted to unbounded domains and are subject to limitations on the boundary conditions. For this reason, a variety of approximate analytical and numerical approaches have been developed to examine domains and boundary conditions that more closely simulate actual growth conditions.

Our work falls into the category of developing analytical approaches for a variety of crystal growing configurations. We have examined time-dependent and steady-state convective-diffusive transport of heat and solute in directional solidification systems. The solution procedure involves a coupled asymptotic/numerical approach. The asymptotic expansions are based upon the assumptions that the ampoule aspect ratio, the heat exchange between the ampoule and sample, and the slope of the liquidus line are small. These scalings lead to boundary layer solutions around the solidifying front. The solidifying interfacial shape, thermal, flow, and solutal profiles are analytically evaluated as functions of the heater temperature profile, heater translation rate, and material properties of the system. The axial and radial segregation, and morphological stability of these systems are predicted.

### **Publications**

1. "Coupled Buoyancy/Morphological Instability in Systems with Small Segregation Coefficient," G. W. Young and S. H. Davis, *Proceedings of the Tenth U.S. National Congress of Applied Mechanics*: Austin, 1986, pp. 237-248.
2. "Directional Solidification with Buoyancy in Systems with Small Segregation Coefficient," G. W. Young and S. H. Davis, *Physical Review B.*, Vol. 34, September 1986, pp. 3388-3396.
3. "Anisotropic Interface Kinetics and Tilted Cells in Unidirectional Solidification," G. W. Young, S. H. Davis, and K. Brattkus. *Journal of Crystal Growth*, Vol. 83 (1987), pp. 560-571.
4. "Morphological Instabilities in Directional Solidification of a Binary Alloy: End Effects," G. W. Young and S. H. Davis. *SIAM Journal on Applied Mathematics* Vol. 49 (1989), pp. 152-164.
5. "Steady-State Thermal Solutal Diffusion in a Float Zone," G. W. Young and A. Chait. *Journal of Crystal Growth*, Vol. 96 (1989), pp. 65-95.
6. "Morphological Instability in a Float Zone," L. B. Humphreys, J. A. Heminger, and G. W. Young. *Journal of Crystal Growth*, Vol. 100 (1990), pp. 31-50.
7. "Surface Tension Driven Heat, Mass, and Momentum Transport in a Two-Dimensional Float-Zone", G. W. Young and A. Chait, *Journal of Crystal Growth*, Vol. 106 (1990), pp. 445-466.
8. "Steady State Thermal-Solutal Convection and Diffusion in a Simulated Float Zone", G. W. Young and A. Chait, *Low-Gravity Fluid Dynamics and Transport*

*Phenomena*, edited by Jean N. Koster and Robert L. Sani, Vol. 130 (1990) Progress in Astronautics and Aeronautics, pp. 119-157.

9. "Float Zone Modelling: Transport Phenomena and Morphological Stability", G. W. Young, Proceedings of the *Eleventh U.S. National Congress of Applied Mechanics*, Tucson, Arizona, May 21-25, 1990, *Appl. Mech. Rev.*, Vol. 43, no. 5, Part 2, May 1990, pp. S63-S69.
10. "An Asymptotic Model of the Mold Region in a Continuous Steel Caster", J. DiLellio and G. W. Young, *Metallurgical Transactions*, Vol. 26b (December 1995), pp. 1225 - 1241.
11. "Modeling the time-dependent growth of single-crystal fibers", G. W. Young and J. A. Heminger, *Journal of Crystal Growth*, Vol. 178 (1997), pp. 410 - 421.
12. "Modeling of the Edge-Defined Film Fed Growth Process", G. W. Young and J. A. Heminger, *Journal of Engineering Mathematics*, Vol. 38 (2000), pp. 371 - 390.
13. "An Asymptotic Approach to Mathematically Modeling Ohno Continuous Casting of Cored Rods", S. A. Morman and G. W. Young, *Journal of Engineering Mathematics*, Vol. 38 (2000), pp. 51 - 76.
14. "Comparison of Asymptotic Solutions of a Phase-Field Model to a Sharp-Interface Model", S. I. Hariharan and G. W. Young, *SIAM Journal on Applied Mathematics*, Vol. 62 (2001), pp. 244-263.
15. "Water Equilibration in Vapor Diffusion Crystal Growth", G. W. Young, E. Gray, and A. Chait, *Mathematical Modeling: Case Studies from Industry*, edited by Ellis Cumberbatch and Alistair Fitt, Cambridge University Press (2001), pp. 199-228.
16. "Asymptotic Solutions of a Phase-Field Model for Alloy Solidification", C. B. Clemons, S. I. Hariharan and G. W. Young, *SIAM Journal on Applied Mathematics*, Vol. 82 (2002), pp. 1952-1972.
17. "Simulation of a One-Dimensional Phase-Field Model For Solidification", L. D. Nelson, J. A. Heminger, C. B. Clemons, G. W. Young, and S. I. Hariharan, *International Journal of Applied Mathematical Sciences*, Vol. 2 (2005), pp. 81-96.
18. "Asymptotic Solutions for a Time-Dependent, Axisymmetric Directional Solidification System", J. Bonfiglio, J. McHood, C. B. Clemons, D. Golovaty, and G. W. Young, *Journal of Crystal Growth*, Vol. 285 (2005), pp. 415-426.
19. "Asymptotic Solutions for an Axisymmetric, Stagnant Film Model of Directional Solidification", C. B. Clemons, D. Golovaty, and G. W. Young, *Journal of Crystal Growth*, Vol. 289, Issue 2 (2006), pp. 715-726.

20. "An Asymptotic Analysis for Directional Solidification of a Binary System", K. Kupchella, C. B. Clemons, D. Golovaty, and G. W. Young, *Journal of Crystal Growth*, Vol. 292, (2006), pp. 111-124.

## **Funding**

1. NASA-ASEE Case Lewis Summer Faculty Fellowship Program, Materials Division - Metals Science Branch - Microgravity Applications, June 1 to August 21, 1987, \$9,600.
2. NASA Lewis Cooperative Agreement for MMSL Software and Hardware Development - NASA Grant No. NCC 3-104, (1988 - 1995): \$1,555,618, G. W. Young – PI, S. I. Hariharan.
3. "Modeling of Material Processing Systems" - 1989 Presidential Young Investigator Award 1989: NSF Grant No. DMS-89-57534 (PYI), (1989 - 1994): \$260,896  
Industrial Partners associated with this award:

A. Schulman Inc.:	\$66,876
Apple Computer, Inc.:	\$795
BP America:	\$10,000
General Electric:	\$10,000
SUN Microsystems:	\$2,601
The Timken Company:	\$30,000
IBM Equipment Grant	\$15,624
4. NASA Lewis Cooperative Agreement for Software and Hardware Development in Computational Materials Science - NASA Grant No. NCC 3-494, (1996 - 1998): \$417,996, G. W. Young – PI, S. I. Hariharan.
5. NSF Division of Mathematical Sciences - "Modelling of Material Processing Systems", NSF Grant No. DMS-95-32021, (1996 - 1998): \$58,948.
6. NSF Division of Mathematical Sciences - "Modeling and Scaling of Material Processing Systems" NSF Grant No. DMS-99-72185, (1999 - 2002): \$122,500, G. W. Young – PI, S. I. Hariharan.
7. NASA Glenn Cooperative Agreement for Modeling, Software and Hardware Development for Analytical and Computational Materials Science - NASA Grant No. NCC 3-716, (1999 - 2003): \$570,292, G. W. Young – PI, S. I. Hariharan and C. B. Clemons.