

4.5/(32) $y = \sin x - \tan x$.

domain/intercepts/symmetry/asymptotes/incr-decr/
max-min/concavity-inflec / sketch.

(A) $D = \{ x \mid x \neq \pm \pi/2, \pm 3\pi/2, \pm 5\pi/2, \dots \}$.

(C) $f(-x) = \sin(-x) - \frac{\sin(-x)}{\cos(-x)} = -\sin x + \frac{\sin x}{\cos x} =$

$= -\sin x + \tan x = -f(x) \Rightarrow f(x)$ odd.

$f(x + 2\pi) = f(x)$: $f(x)$ has period 2π .

(B) $x=0 \rightarrow y = 0 - \frac{0}{1} = 0$: y-int. pt is (0,0)

$y=0$ if $\sin x = \tan x \Rightarrow \sin x = \frac{\sin x}{\cos x}$.

only true at $x = n\pi, n=0,1,2,\dots$

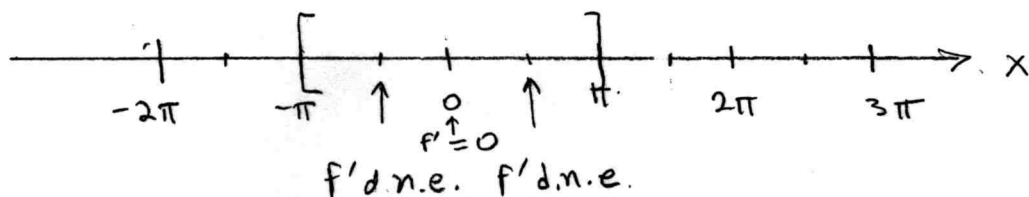
x-int pts $(n\pi, 0), n=0,1,2,\dots$

(D) vertical asymptotes when $\cos x = 0$ or
 $x = \pm \frac{\pi}{2}, \pm \frac{3\pi}{2}, \pm \frac{5\pi}{2}, \dots$ no horiz asy.

(E) $f'(x) = \cos x - \sec^2 x = \cos x - \frac{1}{\cos^2 x} = 0$ if
 $\cos x = \frac{1}{\cos^2 x}$ or $\cos^3 x = 1$. $(\Leftrightarrow) \cos x = 1$.

$\Leftrightarrow x = 0, \pm 2\pi, \pm 4\pi, \dots$

$f'(x)$ d.n.e. if $x = \pm \pi/2, \pm 3\pi/2, \pm 5\pi/2, \dots$



$f'(-\frac{3\pi}{4}) \approx -2.7$

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The fnc is decreasing (not increasing) on its domain.

} checked one period.