

1. Find  $dy/dx$  by implicit differentiation when  $\sqrt{x+y} = 1 + x^2y^2$ .

13 pts

$$\frac{1}{2} \frac{1}{\sqrt{x+y}} (1 + y') = x^2 \cdot 2y y' + y^2 \cdot 2x$$

$$y' \left( \frac{1}{2} \frac{1}{\sqrt{x+y}} - 2x^2y \right) = 2xy^2 - \frac{1}{2} \frac{1}{\sqrt{x+y}}$$

$$y' = \frac{2xy^2 - \frac{1}{2} \frac{1}{\sqrt{x+y}}}{\frac{1}{2} \frac{1}{\sqrt{x+y}} - 2x^2y}$$

2. The equation of motion of a particle is  $s(t) = 2t^3 - 15t^2 + 36t + 2$ , where  $s$  is in meters, and  $t$  is in seconds.

12 pts

(a) Find all critical points of the **VELOCITY** function.

$$v(t) = 6t^2 - 30t + 36 \text{ is diff. on } \mathbb{R}$$

$$v'(t) = 12t - 30 = 0 \text{ if } t = \frac{30}{12} = \frac{5}{2}$$

$t = \frac{5}{2}$  is the only critical #.

(b) What is the acceleration at the times you identified in (2a)?  $a(t) = 12t - 30$

$$a\left(\frac{5}{2}\right) = v'\left(\frac{5}{2}\right) = 0 \text{ m/s}^2$$