

9. Differentiate $y = \sec(\theta) \tan(\theta)$. One way:

10 pts

$$y = \frac{\sin \theta}{(\cos \theta)^2}$$

$$\frac{dy}{d\theta} = \frac{(\cos \theta)^2 \cos \theta - \sin \theta \cdot 2 \cos \theta (-\sin \theta)}{\cos^4 \theta} //$$

$$\begin{aligned} \text{Note} &= \frac{\cancel{\cos \theta} [\cos^2 \theta + 2 \sin^2 \theta]}{\cos^4 \theta} = \frac{\cos^2 \theta + \sin^2 \theta + \sin^2 \theta}{\cos^3 \theta} \\ &= \frac{1 + \sin^2 \theta}{\cos^3 \theta} \end{aligned}$$

10. Calculate $\lim_{t \rightarrow 0} \frac{\sin^2(3t)}{t^2}$. Keep in mind that $\lim_{\theta \rightarrow 0} \frac{\sin(\theta)}{\theta} = 1$.

10 pts

$$\lim_{t \rightarrow 0} 3 \cdot \frac{\sin 3t}{3 \cdot t} \cdot \frac{\sin 3t \cdot 3}{t \cdot 3}$$

(note $3t \rightarrow 0$
as $t \rightarrow 0$)

$$= 9.$$

11. Differentiate $y = \sin(\cos(\sqrt{x}))$.

10 pts

$$\begin{aligned} y' &= \cos(\cos \sqrt{x}) \cdot \frac{d}{dx} (\cos \sqrt{x}) \\ &= \cos(\cos \sqrt{x}) \cdot (-\sin \sqrt{x}) \frac{d}{dx} \sqrt{x} \\ &= -\cos(\cos \sqrt{x}) \sin \sqrt{x} \cdot \frac{1}{2} x^{-1/2} \end{aligned}$$