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11. Consider the function $y = 16/x$. If $x = 4$, and the change in x is $\Delta x = -1$, find the following quantities:

$$f(x) = 16/x$$

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| 6 pts |
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(a) the corresponding change in y (Δy)

$$\begin{aligned}\Delta y &= f(x + \Delta x) - f(x) \\ &= f(3) - f(4) = \frac{16}{3} - \frac{16}{4} = \frac{16 \cdot 4 - 16 \cdot 3}{12} \\ &= 16(4-3)/12 = 16/12 = \boxed{4/3}\end{aligned}$$

(b) the corresponding differential dy

$$\begin{aligned}dy &= \left. \frac{dy}{dx} \right|_{x=4} \cdot dx \\ &= \left. -\frac{16}{x^2} \right|_{x=4} \cdot (-1) = \boxed{1}\end{aligned}$$

12. Find the equations of all the horizontal asymptotes (if any) of the function $f(x) = \frac{x}{\sqrt{x^2+1}}$.

You must use limits to obtain your answer.

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| 8 pts |
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$$\lim_{x \rightarrow \infty} \frac{\overset{1}{\cancel{x/x}}}{\sqrt{\underset{1}{\frac{x^2}{x^2}} + \underset{0}{\frac{1}{x^2}}}}$$

$y = 1$

$$\begin{aligned}x > 0 \rightarrow \\ x &= \sqrt{x^2}\end{aligned}$$

$$\lim_{x \rightarrow -\infty} \frac{\overset{1}{\cancel{x/x}}}{-\sqrt{\underset{1}{\frac{x^2}{x^2}} + \underset{0}{\frac{1}{x^2}}}}$$

$$\begin{aligned}x < 0 \rightarrow \\ x &= -\sqrt{x^2}\end{aligned}$$

$y = -1$